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INVESTIGATION OF EXTENDED BULB ANGLE SECTIONS UNDER COMPRESSION

J. N. SMITH J. N. MURPHY Libr T. S. Naval Postgraduate School Monterey, California







INVLORISTICA OF COURSE OF MOLS

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Fart Two: As Stiffeners attached to sheet

Thesis by

J. N. Smith

J. N. Murphy

In partial fulfillment of the requirements for the Degree of Master of Science in Leronautical Ingineering.

California Institute of Technology
La Jena, California

Thesis 859 C.1

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1. SUMMARY OF RESULTS

PART ONE

This investigation has established the following facts:

- (a) Above an effective length/radius of gyration of about 78, extruded bulb angle sections follow the Euler curve.
- (b) In the short column range the Straight Line Formula gives a more conservative value than the Johnson Parabolic Formula.
- (c) From the experimental data the proportional limit for 24ST extruded sections was found to be 17000 lbs/in².
- (d) When investigating extruded bulb angle sections used as columns for possible local plate failure, since the condition of support at the base of the angle is neither clamped nor simply supported, but an intermediate case, it is suggested that a value of K equal to 1.00 be used in the formula of Timoshenko for plate failure, when the ratio length/width is greater than four. Unfortunately, this suggestion is made on the basis of only two experimental plate failures.



II. STATEMENT OF PROBLEM

At the present time extrusions of various shapes are used in aeronautical construction, replacing sections made up of bent flat sheet. The properties and characteristics of the latter are known with sufficient accuracy; however, very little is known of the behavior of extrusions when acting alone as a column or as a stiffener attached to sheet.

It was considered advisable, before investigating the properties of sheet with attached extruded sections, to look into the behavior of the extruded sections when acting alone in compression.

When a column is acting alone under compression, failure may occur in any of the following ways:

- (a) Failure as an Euler Column.
- (b) Failure by local plate buckling.
- (c) Torsion failure.

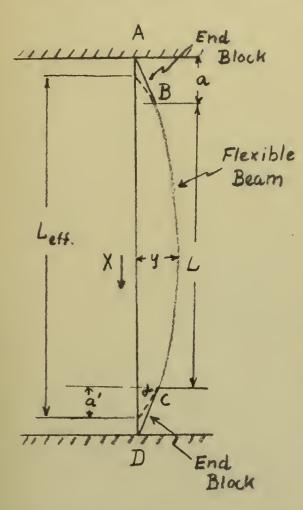
Part One of this research is devoted to an investigation of the behavior of twelve representative extruded bulb angle sections when acting alone as columns.

Part Two of this research is devoted to an investigation of the behavior of extruded sections when acting as stiffeners riveted to sheet.



III. THEORETICAL CALCULATIONS

A development of the theory of effective lengths is reproduced from the Parr-Beakley thesis of 1935. This method was originally deduced by Dr. von Kármán.



The equation for the bending of a beam is

$$EI \frac{d^2y}{dx^2} = -Py \tag{1}$$

the solution of which is

$$y = A \cos \sqrt{\frac{P}{EI}} x$$
 (2)

Boundary Conditions:

AB and CD are supposed to be of infinite rigidity and hence are straight lines, therefore

$$\tan \alpha = -\left(\frac{dy}{dx}\right)_{X} = \frac{L}{2} = \alpha$$

(for small angles)

$$Y_{X} = \frac{L}{2} = a < = -a \left(\frac{dy}{dx}\right)_{X} = \frac{L}{2}$$

or
$$A \cos \sqrt{\frac{P}{EI}} \frac{L}{2} = -a \left[-A \sqrt{\frac{P}{EI}} \sin \sqrt{\frac{P}{EI}} \frac{L}{2} \right]$$

or Cot
$$\sqrt{\frac{P}{EI}} \frac{L}{2} = a\sqrt{\frac{P}{EI}}$$
 (3)



and equation (3) gives the exact value of the P Euler for the case considered.

For a = 0 we obtain
$$\cot \sqrt{\frac{P}{EI}} = 0$$

$$i \cdot e \sqrt{\frac{P}{EI}} \frac{L}{2} = \frac{\pi}{2} \text{ or } P = \frac{\pi^{2}EI}{L^{2}}$$
 (4)

Putting $\frac{F}{EI} \stackrel{L}{2} = Z$ equation (3) may be rewritten

$$Z \tan Z = \frac{I}{2a}$$
 (5)

and
$$\frac{F}{EI} = \frac{2Z}{L}$$

or
$$P = \frac{\Xi I \cdot 4Z^2}{L^2}$$
 (6)

and comparing equation (6) with equation (4) it is seen that the effective length

$$L_{\text{eff}} = L \frac{\pi}{27} \tag{7}$$

therefore:

$$a' = \frac{1}{2} (L_{eff} - L) = \frac{L}{2} (\frac{\pi}{27} - 1)$$

or substituting from equation (5):

$$a' = a\left(\frac{7}{2} - Z\right) \tan Z \tag{I}$$

and from (5)

$$\frac{a}{L} = \frac{1}{2 Z \tan Z}$$
 (II)



and so, if we take different values of Z we can calculate corresponding values of a' and $\frac{a}{L}$.

<u>Z</u>	tan Z	a/L	a'/a
7 2	∞	0	1.0
17 T 36	11.43	0.029	0.999
5 TT 12	3.732	0.102	0.982
<u>π</u> 3	1.732	0.275	0.907

It may be seen from the table that even where the rigid block equals 27.5% of the length of the beam proper, 90.7% of the length of the rigid portion is to be added to the length of the beam to give the effective length.

We will now apply this theory to the research problem (Fig.1). at hand. From the data above, plot a curve of a/L vs a'/a
We obtain:

<u>a</u>	<u>T</u>	a/L	a'/a (from curve)
1.125	22	0.0512	0.996
1.125	16.5	0.0682	0.992
1.125	11	0.1023	0.982
1.125	5.5	0.2045	0.9417



To find L effective:

Knowing the column effective length it is now possible to proceed with a study of the theoretical curves of failure.

In the long column range we shall use the Euler formula:

$$\sigma_{\rm cr} = \frac{c \pi^2 \Xi}{\left(\frac{L_{\rm eff}}{\rho}\right)^2} \tag{1}$$

where C = 1.0

In the short column range both the Johnson Parabolic formula and the "Straight-Line" formula were plotted, (Fig. 2)

$$\sigma_{\rm cr} = \sigma_{\rm y} - \frac{\sigma_{\rm y}^2 \left(\frac{\rm Leff}{\rho}\right)^2}{4\pi^2 E} \tag{2}$$

$$\sigma_{cr} = 48000 - 400 \left(\frac{L_{eff}}{\rho}\right) \tag{3}$$

Investigations by W.L. Howland at California Institute of Technology have placed the proportional limit of aluminum alloys at 19000 lbs/in² (24ST). Our investigations offer



an opportunity to check this value, since at this stress the experimental points should separate from the Euler curve.

This has been carried out approximately as follows: Knowing the value of $L_{\rm eff/p}$ at which the experimental points leave the Euler curve we may solve for

$$\sigma_{p.1} = \frac{\pi^2 E}{\left(\frac{\text{Leff}}{\rho}\right)^2}$$

$$\sigma_{p.1} = \frac{\pi^2 \times 10.500.000}{(78)^2}$$

$$\sigma_{p.1} = \frac{17050 \text{ lbs/in}^2}{2}$$

Investigation into plate failure of the plain angle leg.

Prom Timoshenko: Specimen 8477

$$\sigma_{cr} = k \sigma_{e}$$

$$\sigma_{e} = \frac{\pi^{2}}{12(1-\mu^{2})} \left(\frac{t}{b}\right)^{2}$$

$$\frac{a}{b} = \frac{7.62}{1.25} = 6.1$$

$$t = \frac{1}{2} \left[\frac{3}{32} + \frac{1}{16}\right] = \frac{0.078}{b} \frac{t}{b} = 0.062$$

$$\sigma_{e} = \frac{\pi^{2} \times 10.500.000}{12.3 \times .93} (.062)^{2} = 35800$$



If we assume three sides simply supported and the fourth free, we get

k 2 0.5

$$\sigma_{\rm cr} = 0.5 \times 35800 = 17900 \, {\rm lbs/in}^2$$

If we assume two opposite sides simply supported, the third built in, and the fourth free, we get,

k = 1.33

$$\sigma_{\rm cr} = 1.33 \times 35800 = 47600 \, {\rm lbs/in}^2$$

Now experimentally we find a cr of 37400 lbs/in and therefore we see that we have neither simple support, nor rigid clamping at the side which is supported by the other leg, but as we should expect, something between the two. If we use this cr we may find the experimental value of K for this case:

$$K = \frac{37400}{35800} = 1.044$$

Investigation of Specimen 6478 for plate failure.

$$t/b = \frac{.062}{1.0} = 0.062$$
 $(t/b)^2 = 0.00384$

$$a/b = \frac{7.62}{1.0} = 7.62$$



$$\sigma_{cr} = k\sigma_{e}$$

$$\sigma_{e} = \frac{\pi^{2}}{12(1 - \mu^{2})} \left(\frac{t}{b}\right)^{2} = \frac{35700}{12(1 - \mu^{2})}$$

As in the preceding case we may solve for the experimental value of K. In this case $\sigma_{\rm exp.=34400}$.

$$k = \frac{34400}{35700} = 0.965$$

Unfortunately we experienced only two plate failures. However, if we use the mean value of K determined above, we can check other specimens (which failed as columns) to see if the plate failure stress is higher, thus checking the possibility of that stress being critical.

If we check specimen 10282, which failed as a column at a stress of 15780 lb/in², for plate failure with our experimental value of K equal to 1.0, we find:

t = .04
b = .50
K = 1

$$\sigma_{cr} = \frac{1 \times n^2 \times E}{12(1-n^2)} \left[\frac{.04}{.5} \right]^2$$

$$\sigma_{cr} = 60700 \text{ lbs/in}^2$$

That the stress for plate failure is nearly four times the stress for column failure.



Timoshenko⁽²⁾ gives values of K for a condition when three sides are simply supported and the fourth free, and for a condition when two opposite sides are simply supported, the third side built-in, and the fourth free. For a bulb angle section neither condition describes the actual condition of the side at the base of the angle because, since it is attached to the other leg, it cannot be considered hinged, nor can it be considered fixed, since the latter would imply complete rigidity which is not the case. Apparently then the condition that describes the support of the side at the base of the angle lies somewhere between these two conditions. Our average experimental value of K confirms this assumption.

It is suggested that when bulb angle sections are used alone as columns under compression and pending further investigation, the value of K (as used by Timoshenko in Strength of Materials, Vol. II) be taken as 1.00.



IV. EXPERIMENTAL INVESTIGATION

(a) Description of specimens:

The various bulb angle sections used in aircraft construction by several of the major aircraft manufacturers. were examined and from the lot a representative group of twelve was chosen for this investigation. All of the specimens chosen were 24ST alloy. After giving consideration to current bulkhead spacings between which extruded sections are used as stiffeners and at the same time taking into account the extension into the Euler long and short column ranges, column lengths of 22, $16\frac{1}{8}$, 11, and $5\frac{1}{8}$ inches were chosen for test purposes. In preparing the specimens it was essential that the ends be milled square. It should be noted that, since bulb angle sections are extrusions, their dimensions may vary considerable from those given in the specifications. It was found necessary to check all dimensions and to recompute all the section properties. These properties may vary as much as ten percent from those given in the manufacturer's specifications, (Table 1).

(b) <u>Description of Apparatus</u>:

In order to obtain a true hinged end condition of the columns under test, an end fitting was constructed. A half inch ball-bearing was sunk into the base plate of this fitting, and bears on a circular hardened plate which in turn rests upon the base plates of the compression cage. The ends of the bulb angle are clamped into the fittings where adjustments in



two directions are provided, and ling the controld of the bulb angle to be located directly over the point of the rency of the ball-bearing.

The adjustments is to fittings enable any eccentricity present in the set-up to be removed. Two dial ranges are used to determine if any eccentricity is present. One gauge is mounted on a bracket attached to the cage, the other is held by a rigid bar mounted on flexible tals which in turn are fixed between the circular end plates and the ends of the compression cage. The dial gauge plungers bear on the sides of the bulb angle at the midpoint of the column. Since any restraint of the column is most undesirable it was necessary to remove the plunger main springs of the dial gauges, having only the hair spring acting.

The detail photographs included in the appendix show clearly the construction of the end fittings and the method of setting up the specimens.

(c) Testing Procedure:

The bulb angle is mounted in the end fittings and placed in the compression case. The circular bearing plates are then inserted between the balls and the base plates of the couppression cage. A slight load is applied to the column in order to hold it in the machine and then it is placed approximately vertical by means of a level. The dial gauges are then attached and the load increased, a change in the readings of the gauges



denotes the presence of initial eccentricity which is removed by the adjustments in the end fittings. When the load can be increased to about a third of the anticipated final load without a change in the dial gauge readings it is assumed that all initial eccentricity has been removed. The dial gauges are now removed and the load increased steadily until failure. The tests were made on two Riehle Brothers testing machines, the longer columns in the 3000 pound capacity unit and the shorter columns in the 30,000 pound capacity unit. The type of failure, load, and description of the specimen were recorded.



V. DISCUSSION OF EXPERIMENTAL RESULTS.

In any open section tested as a column under compression three types of failures may be encountered, i.e. column, plate and torsion. Only two of these three possible types of failure occurred in this investigation, column and plate. Of the forty-eight specimens tested, forty-five failed as columns, two $(5\frac{1}{2}$ inch length) as plate failures, and one $(5\frac{1}{2}$ inch length) as a column failure of the bulb alone.

The plain legs of the two specimens which failed from plate failure show a relatively thin section. The theoretical calculations of section III show this type of failure to be critical for these specimens. It is interesting to note that the one specimen of the series whose bulb was on the reverse side, that is, outside of the opening between legs, failed as a column failure of the bulb alone.

During the tests great care was exercised in order to obtain, as nearly as possible, a fixity of unity, and to remove, as far as possible, any initial eccentricities. It appears from the attached curves that we were successful within the limits of experimental error, (Fig. 2).

Unfortunately the opportunities were very limited as regards the investigation of plate failure. However, the two specimens which so failed have been analyzed under the section devoted to theoretical calculations.

No torsion failures were encountered in the specimens tested.



VI. CONCLUSIONS.

The material with which this part of the research problem was performed was not entirely satisfactory, due to the fact that the investigators had no control over the parameters involved. The bulb angle section, being an extrusion, had to be taken as it could be obtained from the Industry. While probably not warranted, it would be desirable from a research point of view, to have a special series of dies, thus permitting a series of specimens in which one dimension could be varied holding the others constant. This would permit a more systematic study of the effect of changes in the parameters and should enable a prediction of an optimum cross-section.

From the investigation as carried out the following conclusions may be listed:

- (1) Above a value of $L_{effective/\rho} = 78$ the Euler curve is followed closely, (Fig.2).
- (2) Below this value of $L_{\rm eff/p}$ the straight line formula (σ = 48000 400 $L_{\rm eff/p}$) appears to approximate the experimental points more closely than the Johnson parabolic formula.
- (3) The proportional limit for 245T extrusions is approximately 17000 lbs/sq.in.
- (4) When investigating the plain leg of the bulb angle section for local plate failure the following experimental



value of K for use in the formulae of Timoshenko more nearly describes the condition of support at the base of the angle.

K (Timoshenko) = 1.00



FART ONE, TABLE I

Comparison of dimensions and areas of extruded bulb angle sections as actually measured and computed, with those taken from the blue prints of the manufacturer.

As measured and computed

Section	(Alcoa	No.)	A	В	R	T ₁	T ₂	Area
8477 8476 8476 8476 10265 10265 10282 3046 5436 12224 K- 4200 K-766 12678			1.125 1.500 1.125 1.000 .875 .750 1.500 1.500 1.094 1.094 .879	1.250 .687 1.000 .688 .500 .500 .568 .996 .625 .624 .499 .445	.125 .113 .109 .095 .094 .067 .082 .156 .125 .118 .095	.138 .051 .073 .059 .052 .047 .052 .104 .105 .078 .062	.087 .055 .061 .065 .056 .042 .058 .079 .103 .084 .067	.2774 .1501 .1679 .1220 .0931 .0647 .1252 .2470 .1709 .1334 .0856 .0402
		As	taken	from the	bluepr	ints of	the manufa	acturer
8477 8476 8478 K-10266 10265 10282 3046 5436 12224 K-4200 K-766 12678		1 1 1 1	.125 .500 .125 .000 .875 .750 .500 .500 .094 .094 .875 .500	1.250 .687 1.000 .687 .500 .500 .5625 1.000 .625 .625 .500 .438	.125 .109 .109 .094 .0625 .075 .156 .125 .1094 .0625	.125 .051 .072 .0625 .051 .040 .050 .125 .1094 .0781 .0625	.0625 .051 .062 .0625 .051 .040 .050 .094 .1094 .0781 .0625	.256 .144 .168 .122 .090 .057 .1154 .32152 .20485 .15555 .10399 .04476



I. ST. M. WANT OF PROBLEM

Extrasions of verious shapes riveted to sheet to give added stiffness and rigidity, are used of tonsively in aeronautical construction, gradually replacing sections made up formed flat sheet.

For this part of the research one of the extruded bulb angle sections which was investigated for its column properties in part one, was chosen for the stiffener to be riveted to the sheet.

The bulb angle section and the sheet which were used to make the panels, were 24°T alloy.

II. DESCRIPTION AND TABULATION OF FAMILS

For the stiffener in the panel, bulb angle section alcoa number 10282 with a cross-sectional area of .0347 square inches and a radius of gyration of .27 inches, was selected. For all panels the stiffener spacing was taken as 4 inches and the rivet spacing as .75 inches (4). Two thicknesses of sheet were used, namely, .02 and .04 inches. Fanels of two, three, and four stiffeners were made and tested, using the above spacings and thicknesses of sheet. In order to cover the current range of bulkhead spacings and at the same time extend into both the Buler long and short column ranges, the lengths of the panels chosen for test purposes were 7, 5%, 11, 16%, 22, and 27% inches. In each panel the shoot extended 2 inches teyond each outboard stiffener, that is, the width of the panel with two stiffeners was 8 inches; three stiffeners, 12 inches; four stiffeners, 11 inches.



The following tabulation describes the panels which were tested:

No.of stiff.	Sheet thick.		Panel len.	Panel width	Stiff. area	Sheet	Total	Total load	Average stress
222222222233333333344444444444444444444	.02 .02 .02 .02 .02 .04 .04 .04 .04 .04 .04 .04 .04 .04 .04	444444444444444444444444444444444444444	3 5 1 6 2 7 3 5 1	8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	.1294 .1294	.16 .16 .16 .16 .16 .16 .16 .16 .16 .16	2894 2894 2894 2894 2894 2894 4494 4494	6250 6550 5310 6170 6160 5040 9460 11080 9150 10080 11150 9830 7675 8915 7602 6650 16170 12290 12870 14010 14938 12240 11855 11450 8720 11390 985 8810 18200 20230 17120	21600 22640 18350 21300 21300 21300 21300 21050 24700 20360 22470 24800 21900 18100 21630 17680 20530 17500 15320 23970 18230 19090 20780 22160 18150 20500 19780 15060 19670 17260 15220 20250 22500 19050
4 4 4	.04 .04 .04	4 4 4	16½ 22 27½	16 16 16	.2588 .2588 .2588	.64 .64	.8988 .8988	18590 17938 14825	20670 19960 16500



III. TETTING PROJEDURE

In tests of this kind it is imperative that the opposite ends be parallel in order to have an even distribution of the load. Ith this in mind the panels were fabricated with a plus allowance in each length, and then placed in the milling machine and milled to the lengths chosen for test purposes.

Before the panel was put in the testing machine, two extensometers were placed on the side of the sheet opposite side to which the stiffeners were attached, and near the point of attachment of the end stiffeners of the panel. From the readings of these extensometers the effective width of the sheet acting with the stiffener can be computed, giving a check on other methods.

as nearly parallel as possible, it was found to be necessary, particularly in the wider panels, to shim the ends in order to obtain an even distribution of the load. When the panel was placed in the testing machine a slight load was applied and, if necessary, shims were inserted until it seemed apparent that the load was evenly distributed along the width of the panel. The load was then increased until the panel failed. In addition to the extensometer readings and failure load, the general behavior of each panel was recorded, noting in particular the first appearance of waves in both sheet and stiffener and the passage of waves through the rivet specific. The latter effect was not pronounced or consistent and failed, in many cases, to leave a permanent set in the rivet line.



IV. CALCULATIONS

In order to plot the Euler curves, (Figs. 1,2,3), it is necessary to know the amount of sheet theoretically acting with the stiffener and the end load carried by the end tubes. The total Euler load will then be given by the formula,

Pend is obtained readily from the curve giving the experimental "faired" values of P, (Fig.6). In order to obtain consistent results a cross-plot was made. First values of P were plotted vs. number of stiffeners, (Figs. 4,5), then from the faired curves a second plot was made of P vs. length. These curves are included in the appendix, (Fig.6).

As an example P_{end} will be calculated for the $27\frac{1}{2}$ inch, 0.020 thickness panel.

where subscript s+s refers to stiffener plus effective sheet.

$$P_{2} = 4800 = 2P_{s+s} + 2P_{end}$$

$$P_{3} = 6850 = 3P_{s+s} + 2P_{end}$$

$$P_{\text{end}} = \frac{4800 - 4100}{2} = 350 \text{ lbs.}$$



This method is followed for all panel lengths, sheet thicknesses, and stiffener combinations. Since there will be some scatter a curve was faired, through the plotted values of P_{end}, (Fig.7), and the mean values used to find the Euler load.

It is now necessary to determine the Euler stress (σ_{E}) of the stiffener alone, for two values of end fixity, i.e. k = 2 and k = 3.

$$\sigma_{\rm E} = \frac{k \pi^2 g}{(L/\rho)^2}$$

$$\rho = 0.27$$

Tabulating the results, we obtain:

<u>L</u>	L/p	(L/p)2	2 T 2 E	3 T 2 E	$\sigma_{\underline{E}(K=2)}$	$T_{E}(K = 3)$
27.5	102	10400	207,300,000	310,500,000	19,900	29,800
22.0	81.5	6640	207,300,000	310,500,000	31,100	46,800
16.5	61.0	3720	207,300,000	310,500,000	55,600	83,500
11.0	40.8	1665	207,300,000	310,500,000	124,000	186,400
5.5	20.4	416	207,300,000	310,500,000	497,000	746,000
3.0	11.1	123	207,300,000	310,500,000	1,680,000	2,520,000

We can compute constants for use in the two curves drawn by Dr. E. E. Sechler of the Institute, (Figs. B-2,B-3, taken from reference (3)).

$$\lambda = t/b\sqrt{1/\sigma} = \frac{3235t}{b}\sqrt{1/\sigma}$$

for 0.020" sheet

 $\lambda = \frac{13.2}{\sigma_{2}}$
 $t/a_{0} = 0.309$

where $A_{0} = 0.0647$ (for 10282 stiffener)

 $3/\rho_{0} = 1.15$



The method of using the curves will be shown by working one length.

L = 27.5"

t = 0.020"

K = 2

 $\sigma_{\rm E}$ (from preceding page) = 19900 lbs/in²

 $O^{\frac{1}{2}} = 141$

 $\lambda = \frac{16.2}{141} = 0.115$

Entering curve of effective widths, (Fig. B-2); in this case we are on the transition curve between A and B.

 $W_{e/b} = 0.265$

b = 4 (stiffener spacing)

2We = 2.12

From Fig. B-3 we obtain

% = 0.92

 $\sigma_{1} = 19900 \times .92 = 18300$ lbs/in²

σ₁½= 135

 $\lambda = 0.12$

 $W_{e/b} = 0.265$

27/e = 2.12

T/0 = 0.92

The correct values of G and $2W_e$ are therefore 18300 lbs/in² and 2.12 inches. We know this to be approximately correct since the ratio G remains the same. The tabulated results can be found in Table II Appendix.



The theoretical values of P can now be calculated using the curves of Pend vs. length, (Fig. 7 and table II).

Sample Calculation:

L = 27.5 inches t = 0.020"

O = 18300 lbs./in²

n = number stiffeners =2

 $A_{S+S} = 0.0647 + 2.12 \times 0.02 = 0.1071$

 $P = n \times \Lambda_{s+s} \times \sigma + 2P_{end}$

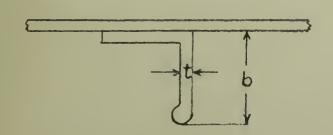
P = 2 x 0.1071 x 18300 + 2 x 230

P = 4380 lbs.

Plate Failure of the Outstanding Stiffener Leg.

In discussing this subject we shall follow the method of Timoshenko (Vol. II, Strength of Materials) and will attempt to determine a value of K which will suit the conditions of support of the panels tested. We know that none of the conditions of support for which Timoshenko has tabulated values of K exactly fit our case. In our panels we have three sides in which the fixity varies between a simple support and a built-in condition and a fourth side which is not entirely free due to some restraint provided by the bulb of the bulb angle section.

From our results we will determine an experimental value of K.



Length of Panel : a t = 0.047



$$\mathcal{T}_{cr} = K \mathcal{T}_{e}$$

$$\mathcal{T}_{e} = \frac{\pi^{2} Et^{2}}{12b^{2} (1-\mu^{2})} = \frac{\pi^{2} \times 10,500,000 \times (0.047)^{2}}{12 \times (0.75)^{2} \times (1-.09)}$$

$$\mathcal{T}_{e} = \frac{228,000}{6.14} = 37150 \text{ lbs/in}^{2}$$

It must be noted at this point that $\sigma_{\rm cr}$ is the actual critical stress in the stiffener leg. It will probably always be difficult to predict this stress from the average stress in the panel or from the compressive load and the geometry of the cross-section. We have, therefore, defined $\sigma_{\rm cr}$ as the average stress in the panel at failure.

It is felt that this definition will permit the engineer to work entirely with knownquantities: An experimental value of K will now be determined, using the properties of the three-stiffener section. This K will be tabulated for different values of a/b and checked by predicting the failure load for several of the panels with two and four stiffeners.

Method of obtaining K:

L = a = 3" b = 0.75" a/b = 4.0

thickness sheet = 0.020"

$$\sigma_e = 37150 \text{ lbs/in}^2$$

Atotal = 3 Astiffener + Asheet = $3 \times .0647 + .02 \times 12$

 $A_{t} = 0.4341$

P = 8700

 $\sigma_{cr} = \frac{8700}{4341} = 20050 \text{ lbs/in}^2$

 $K = \frac{20050}{37150} = 0.540$



3 - Stiffeners

$$a/b = 4.0$$

thickness sheet = 0.040"

 $\sigma_e = 37150 \text{ lbs/in}^2$

 $A_{t} = 3 \times .0647 + .04 \times 12$

P = 14700 los.

 $\sigma_{\rm cr} = \frac{14700}{6741}$ = 21800 lbs/in²

 $K = \frac{21800}{37150} = 0.587$

And similarly for other values of a/b.

Table of K for various values of a/b

thickness of sheet - 0.020"

$$a/b = 4.0$$

thickness of sheet - 0.040"

$$a/b = 4.0$$

The reason for this difference in K with varying sheet thicknesses is probably due to the increase in end fixity with increasing sheet thickness.

It should now be possible to use these values of K and predict Tcr and hence the load at failure. We will do this as a check on K by working out a theoretical P for several panels with two and four stiffeners, comparing the value obtained with the actual load at failure.



It should be noted that σ_e is a constant for any given stiffener. In the case of the 10282 section used in this investigation, $\sigma_{\rm e}$ = 37150 lbs/in².

Checking values of K:

$$a = 16.5$$
"

$$K = 0.521$$

$$\sigma_e = 37150 \text{ lbs/in}^2$$

$$\sigma_{cr} = K \sigma_{e} = 0.521 \times 37150 = 19350 \text{ lbs/in}^2$$

$$A_{t} = 2 \times 0.647 + .02 \times 8 = .2894$$

$$b = 0.75^{\circ}$$
 a/b = 7.35

$$K = 0.585$$

$$\sigma_e = 37150 \text{ lbs/in}^2$$

$$\sigma_{cr} = 0.585 \times 37150 = 21700 \text{ lbs/in}^2$$

$$A_{t} = 2 \times .0647 + .04^{\circ} \times 8 = .4494$$



Checking values of K:

$$b = 0.75$$
"

$$b = 0.75$$
" $a/b = 4.0$

$$K = 0.54$$

$$A_{t}$$
= 4 x .0647 + .02 x 16 = .5788

$$b = 0.75$$
"

$$K = 0.546$$

$$A_{t} = 4 \times .0647 + .04 \times 16 = .8988$$

From our results in general it is believed that these values of K will give conservative results.



V. DISCUSSION OF EXPERIMENTAL RESULTS

The behavior of the panel while under test was interesting. The formation of waves, while the same in both thicknesses of sheet, was much easier to see in the 0.020" panels. Under a relatively low load a slight wave is first noticed in the sheet between stiffeners. As the load is increased the waves in the sheet become deeper and extend closer to the stiffeners, while the outstanding leg of the stiffeners goes into a wave form. Near failure the waves in the sheet go through the rivet line of the stiffeners and the waves in the outstanding leg become pronounced. In every panel tested failure resulted from a plate failure of the outstanding leg of the stiffener. In the 27.5" panels a tendency was noted for the panel to fail as an Euler column, however, the critical condition was still a plate failure of the outstanding stiffener leg.

From the curves, (fig. 1,2,3) the actual end fixity was estimated. This was done by plotting Euler curves for different values of fixity and observing where the faired experimental curves became tangent to the Euler curves. The end fixity of the panels tested was: 2.7 for the 0.020 sheet thickness and 3.2 for the 0.040 sheet thickness.

From our investigation it would appear that for the particular combination of sheet, stiffener and rivet spacing used an empirical value of k can be determined. This value of k is used in the formulae given by Timoshenko (Strength of Materials, Vol. II, page 605). The definition of $\sigma_{\rm cr}$ as the



average stress in the panel at failure is, we believe, justified since it is that stress which the designer will calculate in any application to stressed skin structures. Since σ_e is a constant for a particular stiffener; it is only necessary to look up k, entering table IV with the ratio

The value of Gr may then be calculated from the formula:

If the average stress (using whole area) is equal to or above σ_{cr} the panel will fail due to plate failure of the outstanding leg of the stiffener. It is suggested that more work be done along this line, using other stiffener, sheet combinations, and attempting to achieve an end fixity which will closely approximate those found in the actual structure of the airplane.



VI. CONCLUSIONS

- (1) It will be evident from an examination of Figures 1, 2, and 3, that the experimental values for the eleven inch panels fall considerably below the faired curves. This error is consistent, and is present in all combinations of sheet thicknesses and number of stiffeners tested in this length. There is no explanation for this behavior and lack of time prevented a re-check by the authors. It is recommended that the eleven inch points be regarded with doubt and checked by the personnel assigned to this research next year.
- (2) The end fixity for the panels tested was found to be:
 - 2.7 (sheet thickness of 0.020")
 3.2 (sheet thickness of 0.040")
- (3) For the type of bulb angle section used as stiffener in these tests an experimental value of K has been determined, (table IV). The proper value of K, taken from table IV, is to be used in Timoshenko's formulae (Strength of Materials, Vol. II, page 605), with modifications as outlined in Section IV of this paper. Following the method given, a close approximation will be obtained for the load at which plate failure of the outstanding leg occurs.
- (4) There was no tendency for the type stiffener used in these tests to fail in torsion.



- (5) Extensometer readings were taken during all tests. From these readings the theoretical value of the effective width of sheet acting with the stiffener could be checked. The authors were unable to carry this project through in the time available and it is suggested that it be done at a later date by the group assigned to a like problem next year.
- (6) It is recommended that this project be carried on following similar lines. It would be desirable to test at least two panels in each length, sheet thickness, and number of stiffeners. The eleven inch lengths in the panels tested by the authors should again be tested and a check made of the values obtained in this investigation. Due to the great importance of this type of construction in the Industry it is suggested that as many of the remaining eleven bulb angle sections (see Part One) be attached to sheet and tested as time will allow.
- of K obtained for the outstanding leg and which should also be investigated is the ratio of the bulb area to the area of the outstanding leg of the section. This ratio will determine to a large extent the amount of fixity to be assigned to the outstanding leg and therefore determine to a large extent the value of the constant K.



affENDIX

REFERENCES

- (1) Parr-Beakley Thesis of 1935.
- (2) S. Timoshenko Strength of Materials, Vol. II, page 606.
- (3) Compressive Stress Distribution of Stiffened Sheet Panels, Dr. E. Sechler, Journal of the Aeronautical Sciences, June, 1937.
- (4) Effect of Rivet Spacing on Stiffened Thin Sheet Under Compression, M. L. Howland, Journal of the Aeronautical Sciences, October, 1936.



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	2120	3540	7210	21700	2365	3460	7980	24000	2310	3865	1770	23400	8390	14070	28300	85000	3585	0109	12070	36350
	961	335	615	1540	147	210	410	1025	294	405	200	1945*	2230	3445	6040	3605	820	1180	2320	5840
	661	334	1691	2020	153	256	515	1552	289	484	973	2930	2070	3470	0867	21000	613	1028	2060	6210
	48400	28900	14400	4800	43700	26080	13000	4310	45000	26900	13350	0444	12380	7370	3670	1225	28750	17150	8520	2840
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	24.24	18.73	13.21	7.62	24.24	18.73	13.21	7.62	24.24	18.73	13.21	7.62	24.24	18.73	13.21	7.62	24.24	18.73	13.21	7.62
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Specimen Ix

Parameters are based on actual dimensions, not on # Indicates a column failure of the bulb alone those listed by the manufacturer.



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acted	2703	4310	7365	10370*	240	875	1670	4020	1490	2275	3875	5770*	469	775	1545	2650
Feuler	2865	4800	9640	29050	587	482	1975	5940	1543	2580	5200	15660	516	1198	1737	5223
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Post.	24.24	18.73	13.21	7.62	24.24	18.73	13.21	7.62	24.24	18.73	13.21	7.62	24.24	18.73	13.21	7.62
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* Indicates plate failure

Parameters are based on actual dimensions, not on those listed by the manufacturer.



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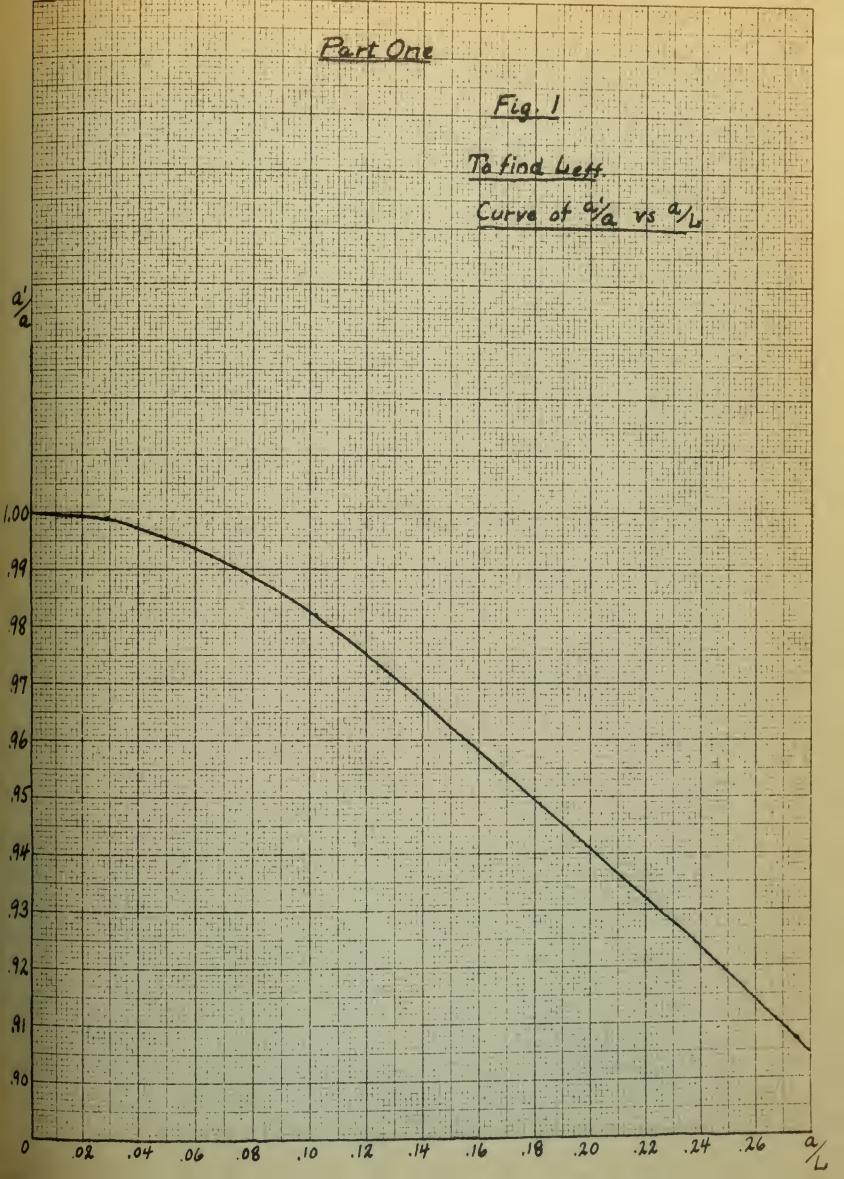






Table I , Part Two

Calculation of Experimental Pstillener + sneet ail Fpanel trong faired curves.

1	Pstiff. + s	heet	ipane	1 .	Avg. Patin	,+3neet	Avg. P	anel
	0.020"	0.040"	0.020	0.040	0.020	0.040	0.020"	0.040
	2300	4000	0	100				
27.5	2100	3900	200	200	2100	3900	267	233
7	1900	3800	600	400				
_	2250	3800	625	1500				
22.0	2175	3800	708	1500	2175	3800	725	1500
,	2100	3800	850	1500				
	2050	3800	1325	1500				
16.5	2125	3800	750	1500	2125	3800	1058	1500
-	2200	3800	1100	1500				
	2200	3800	400	700		•		
11.0	2150	3850	450	650	2150	3850	467	633
	2100	3900	550	550	,			
	2100	3700	1500	1600				
5.5	2060	3800	1550	1500	2050	3800	1567	1467
1	2000	3900	1650	1300				
1	2200	3800	800	2100				
3.0	2100	3850	900	2050	2100	3850	933	2033
	2000	3900	1100	1950				



(enoth	K=2	t = 0.020	K=3	K = 3 t= 0.020	X "X	K=2 t=0.040	K=3 t	K=3 t=0.040
רבוולמו	Ь	2 We	Ь	2 We	Ь	2 We	Ь	2 We
27.5	18300	2.12	24800	1.24	17300	2.45	25600	1.84
22.0	31100	1.18	46800	0.446	26400	1.80	46800	0,88
16.5	55600	0,473	83500	0,384	55600	0.84	83500	0.704
11.0	124,000	0.32	186,400	0,28	126,400	09.0	192,000	0:448
5,5	447,000	0.176	746,000	0,144	511,000	0,32	269,000	0.264
3,0	1,680,000	80'0	2,520,000	0.064	1,715,000	0.178	2,570,000 0.144	0.144

have no practical meaning, being points on the steep The high stresses corresponding to the shorter lengths portion of the Euler curve.



Table III, Part Two

1	<u>T</u> 4	15850	21420	34220	68440	235,180	728,700
t=0.04 K-2	\mathcal{T}_{ω}	12310 15850	16740	26520	48440 35990 52240	82,980 122,700 162,200 119,480 177,280	
t	Tu		12070	19660 25090 18750	35990	119,480	365,700
2	T4	10060 ,12850 8760	17150 12070	25090	48440	162,200	495,700
£=0.04 K=2	5	10060	13540	09961	37140	122,700	372,200
***	54	7270	9930	14180	25940	82,480	249,700
t = 0.02	R*	11140	15400	26270	54890	204,600	667,700
	50	8460	11930	20240	41790	154,100	502,700
K= 3	\mathcal{D}_{n}	5800	8440	14220	28690	103,600	334,700
20	D.*	8330	12430	18320	37790	138,400	447,700
t-0.02	מי	6330	9390	14490	28890	104,640	336,700
K=2	₩.	4380	6940	10370	20110	70540	225,200 336,700 447,700 334,700 502,700 667,700 249,700 372,200 495,700 365,700 546,700
Lenoths	†! 	27.5	22.0	16.5	0.11	5:0	0

The subscript on P indicates the number of stiffeners. These values are used to plot the Euler Curves.

meaning, being points on the steep portion of the Euler curve. The high values of P in the shorter lengths have no practical



Part Two

Table IV

Thickness of sheet = 0.020"

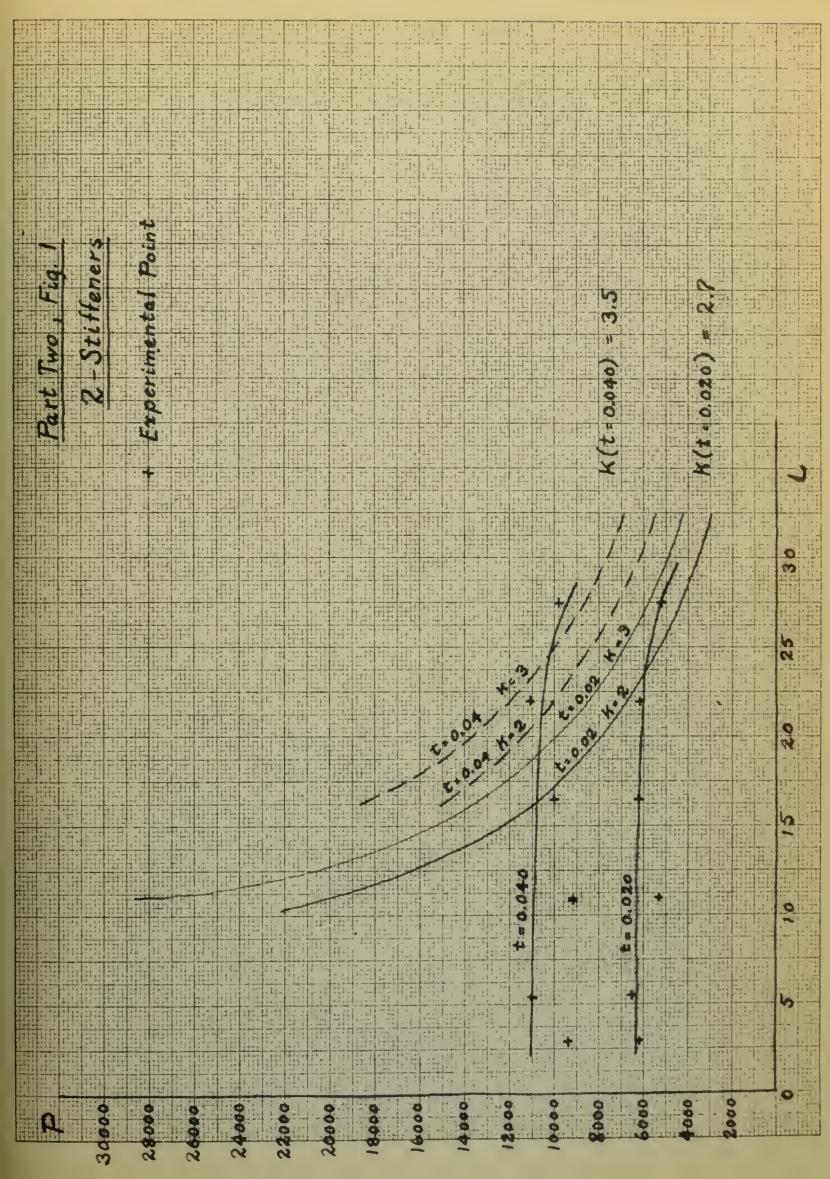
^а/_b 4.0 7.35 14.68 22.0 29.35 36.70 к 0.540 0.537 0.533 0.521 0.502 0.446

Thickness of sheet = 0.040°

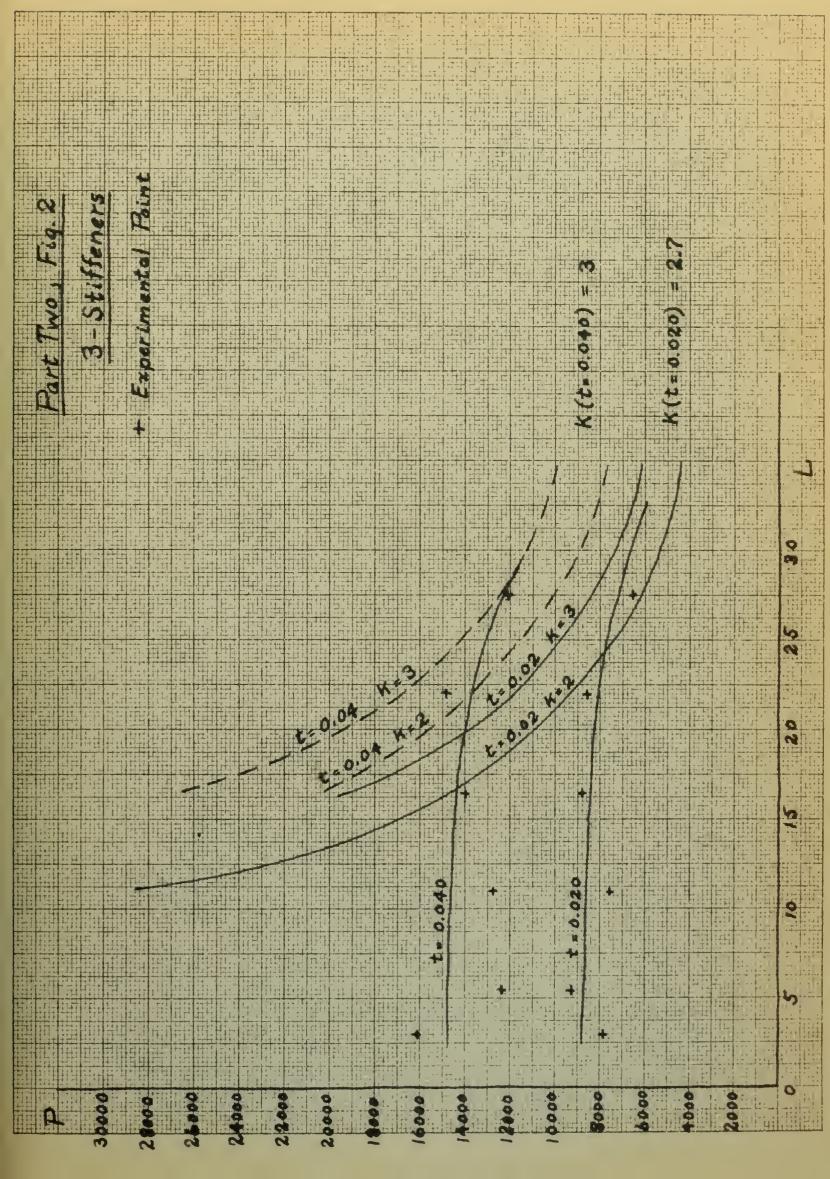
^a/_b 4.0 7.35 14.68 22.0 29.35 36.70 K 0.587 0.585 0.582 0.575 0.546 0.488

These values only apply when using ALCOA number 10282 extruded bulb angle sections as stiffeners.

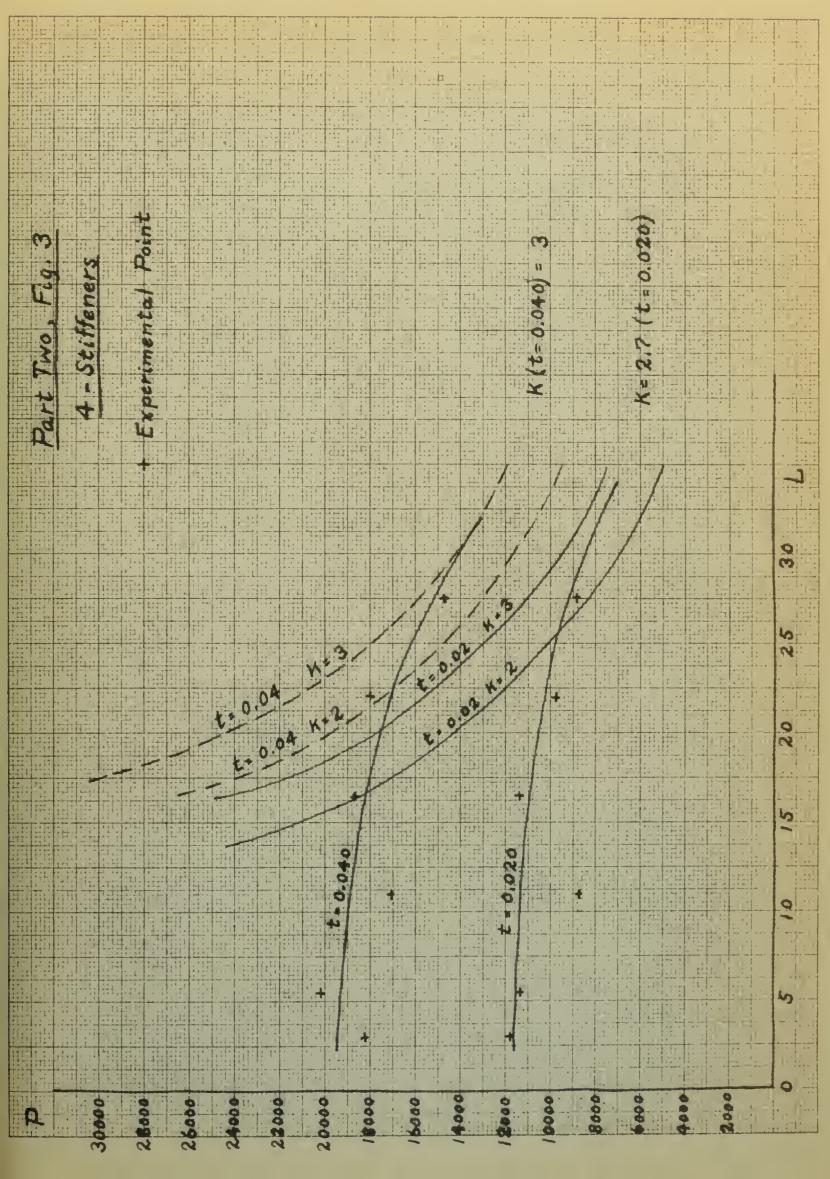












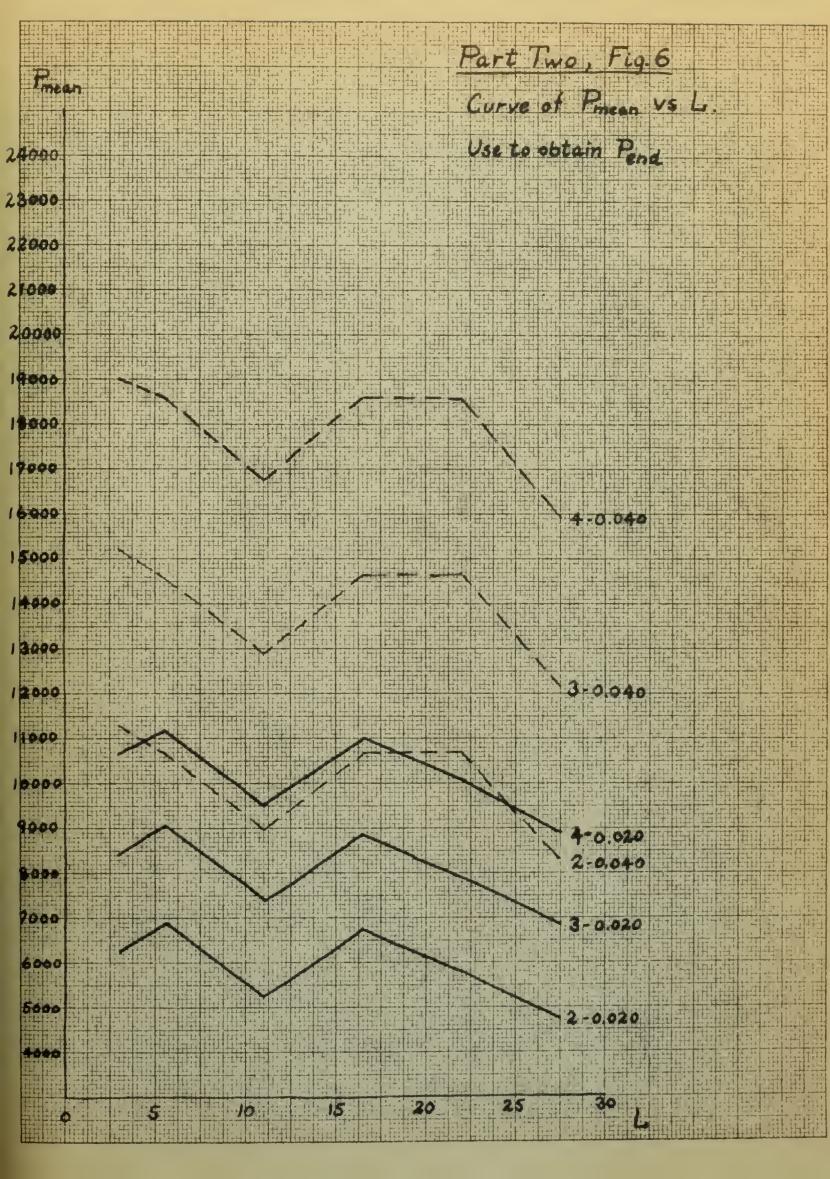


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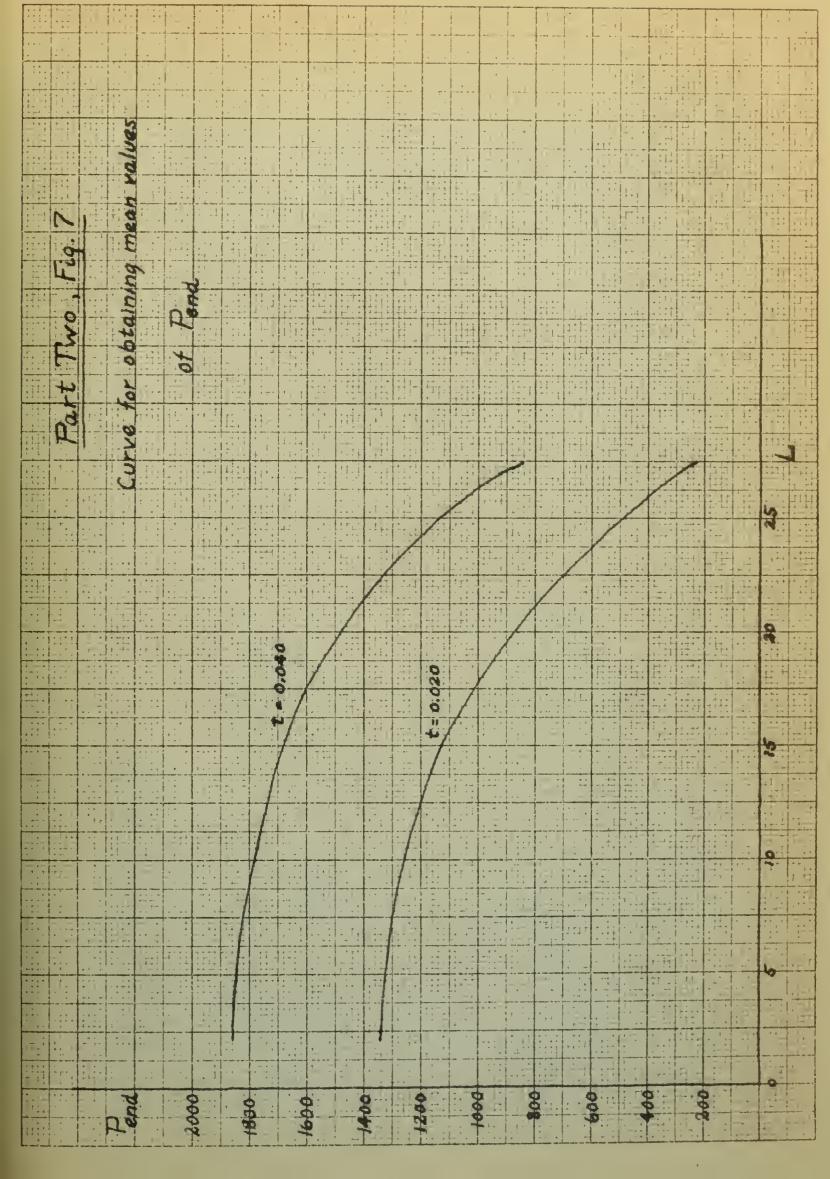


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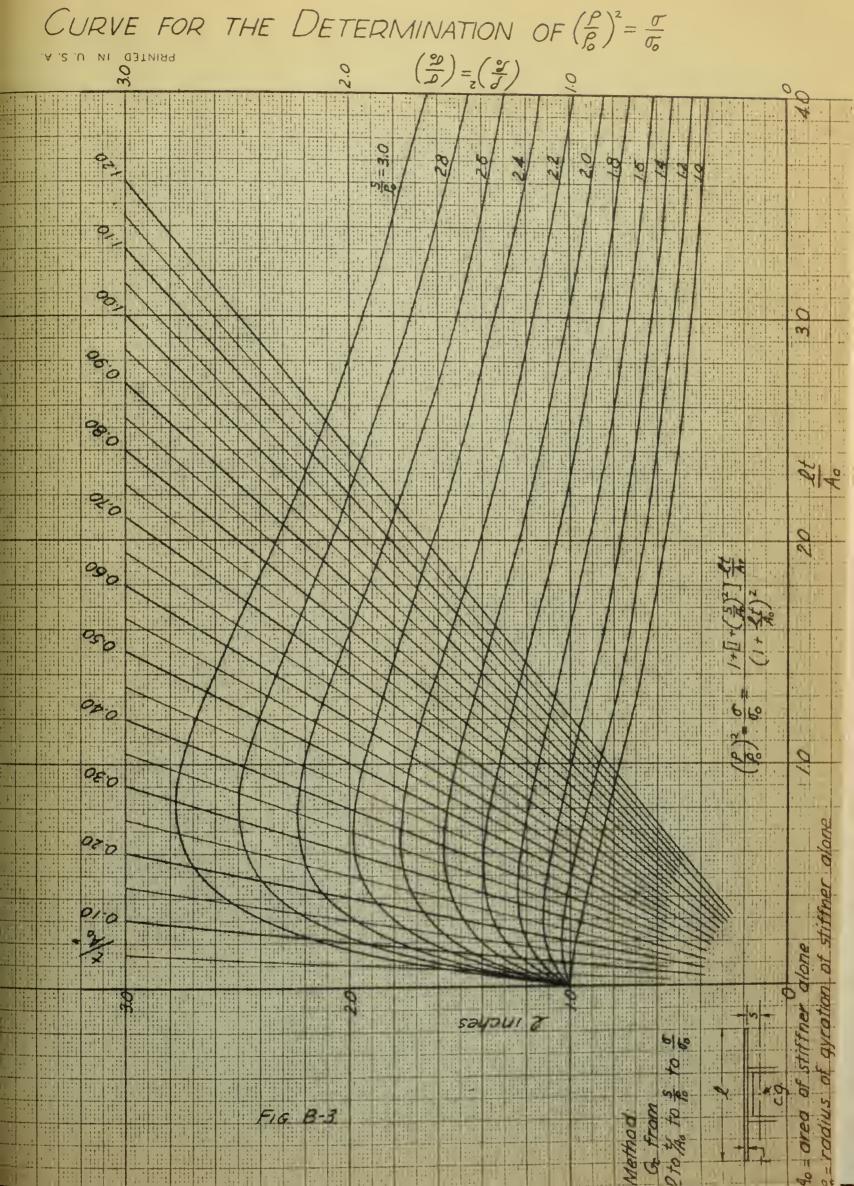






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